

Gravitational force

Gravity is an attractive force between any 2 masses.

On Earth...

$$F = ma \text{ but } a = g$$

$$\therefore \boxed{F_g = mg}$$


Weight = force of gravity on an object

Mass = amount of matter

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In general

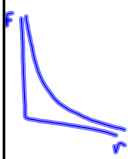
$$F_g \propto m_1 m_2$$

$$F_g \propto \frac{1}{r^2}$$


$$F_g \propto \frac{m_1 m_2}{r^2}$$

$$F_g = \frac{G m_1 m_2}{r^2}$$

G = universal gravitational constant



$$[N] = \frac{[Nm^2]}{[kg^2]} \frac{[kg][kg]}{[m^2]} = 6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$$

Ex. What is the gravitational force between you and the person sitting next to you?

$r = 0.7 \text{ m}$
 $m_1 = 60 \text{ kg}$
 $m_2 = 70 \text{ kg}$

$$F_g = \frac{G m_1 m_2}{r^2}$$

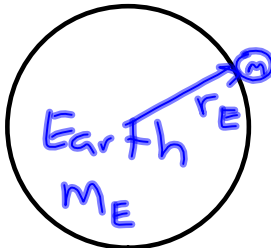
$$= \frac{(6.67 \times 10^{-11})(60)(70)}{(0.7)^2}$$

$$F_g = 5.71 \times 10^{-7} \text{ N}$$

60kg...
 $a = \frac{F}{m}$
 $= \frac{5.71 \times 10^{-7}}{60}$

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We can use this to get g



$$F_g = \frac{G M_E m}{r^2}$$

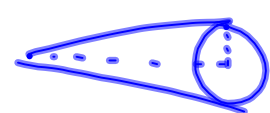
$$F_g = mg$$

$$\therefore \cancel{mg} = \frac{G M_E m}{r^2}$$

$$g = \frac{G M_E}{r_E^2}$$

$$F_g = 9.8m$$

$M_E = 5.98 \times 10^{24} \text{ kg}$
 $r_E = 6.38 \times 10^6 \text{ m}$



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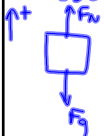
The Normal Force

'Normal' means "at right angles"

$F_N \rightarrow \perp$ the surface
(perpendicular to)

\rightarrow meant to stop object from going through surface

Ex.
A 250 g book sits on a desk...



$$F_{NET} = ma$$

$$= 0$$

$$F_{NET} = \sum F$$

$$= F_N - F_g$$

$$\therefore 0 = F_N - F_g$$

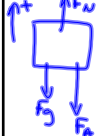
$$\therefore F_N = F_g$$

$$= mg$$

$$= (0.25)(9.8)$$

$$= 2.45 \text{ N}$$

If you push down on the book with a force of 5 N...



$$F_{NET} = 0$$

$$F_{NET} = F_N - F_g - F_A$$

$$\therefore F_N - F_g - F_A = 0$$

$$F_N = F_g + F_A$$

$$= mg + 5$$

$$= (0.25)(9.8) + 5$$

$$= 7.45 \text{ N}$$

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$$F_{NET} = F_N - F_g + 5$$

$$F_{NET} = 0$$

$$\therefore F_N - F_g + 5 = 0$$

$$F_N = F_g - 5$$

$$= (12)(9.8) - 5$$

$$= 117.6 - 5$$

$$= 112.6 \text{ N}$$

Hor.
 $F_{NET} = ma$
 $F_{NET} = 8.66 \text{ N}$
 $\therefore 8.66 = ma$
 $a = \frac{8.66}{12}$
 $a = 0.72 \frac{\text{m}}{\text{s}^2}$

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Friction

Friction is a resistive force that occurs between 2 surfaces.

resistive \rightarrow always opposes motion

2 types of friction:

<p><u>static</u></p> <ul style="list-style-type: none"> - surfaces are not moving against each other Eg. - car is parked - car is driving (under control) <p>Always at least as large as Kinetic</p>	<p><u>kinetic</u></p> <ul style="list-style-type: none"> - surfaces slide along each other - car is skidding <p>Smaller than Static</p>
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F_f is affected by...

- ... the 2 surfaces in contact
- ... the normal force

$F_f \propto F_N$

$F_f = \text{constant} \times F_N$

coefficient of friction μ

Examples

Surfaces	μ_k	μ_s
Steel on steel, dry	0.41	0.6
greasy	0.12	
rubber-asphalt dry	1.07	
wet	0.95	
rubber-concrete dry	1.02	
wet	0.97	

$F_f = \mu F_N$

$\mu = \frac{F_f}{F_N}$

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Example:

A skier is being pulled by a cable with a force of 65 N (30° above the horizontal). If the skier has a mass of 50 kg , and $\mu = 0.1$ between the skis and the snow, what is the skier's acceleration?

Vert:

$$F_{NET} = 32.5 + F_N - F_g$$

$$F_{NET} = 0$$

$$\therefore 0 = 32.5 + F_N - F_g$$

$$F_N = mg - 32.5$$

$$= 457.5\text{ N}$$

Hor.

$$F_{NET} = 56.3 - F_f$$

$$F_{NET} = ma$$

$$\therefore 50a = 56.3 - \mu F_N$$

$$50a = 56.3 - (0.1)(457.5)$$

$$= 56.3 - 45.75$$

$$= 10.55$$

$$a = 0.21 \frac{\text{m}}{\text{s}^2}$$

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