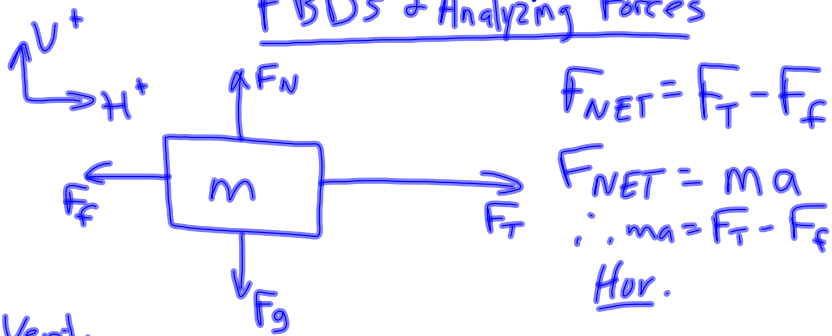


FBD's & Analyzing Forces



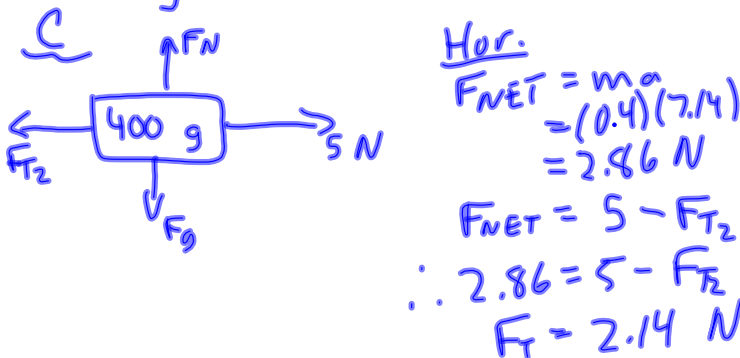
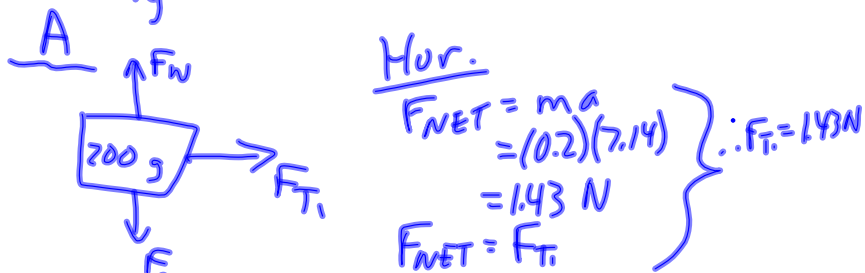
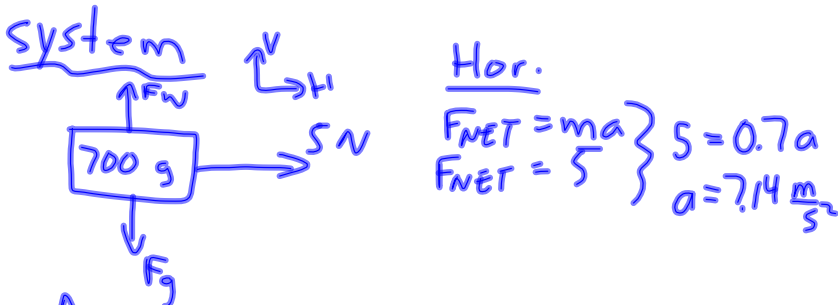
Vert.
 $F_{NET} = 0$
 $F_{NET} = F_N - F_g$
 $\therefore F_N = F_g$

Train Problems...

A series of 3 toy trains is being pulled as shown:



Determine the tension in each of the ropes attaching the trains.



With Friction... $\mu = 0.4$

System

Vert.:

$$F_{NET} = 0$$

$$F_{NET} = F_g - F_N$$

$$\therefore F_N = F_g = (0.7)(9.8) = 6.86 \text{ N}$$

Hor.

$$F_{NET} = 0.7a$$

$$F_{NET} = 5 - F_f$$

$$= 5 - \mu F_N$$

$$= 5 - (0.4)(6.86)$$

$$= 5 - 2.74$$

$$= 2.26 \text{ N}$$

$$\therefore 0.7a = 2.26$$

$$a = 3.22 \frac{\text{m}}{\text{s}^2}$$

A + B

Vert.:

$$F_N = F_g = (0.3)(9.8) = 2.94 \text{ N}$$

Hor.:

$$F_{NET} = ma = (0.3)(3.22) = 0.966 \text{ N}$$

$$F_{NET} = F_{T2} - F_f$$

$$0.966 = F_{T2} - \mu F_N$$

$$= F_{T2} - (0.4)(2.94)$$

$$0.966 = F_{T2} - 1.176$$

$$\therefore F_{T2} = 1.176 + 0.966 = 2.142 \text{ N}$$

B

Vert.:

$$F_N = F_g = 0.98 \text{ N}$$

Hor.:

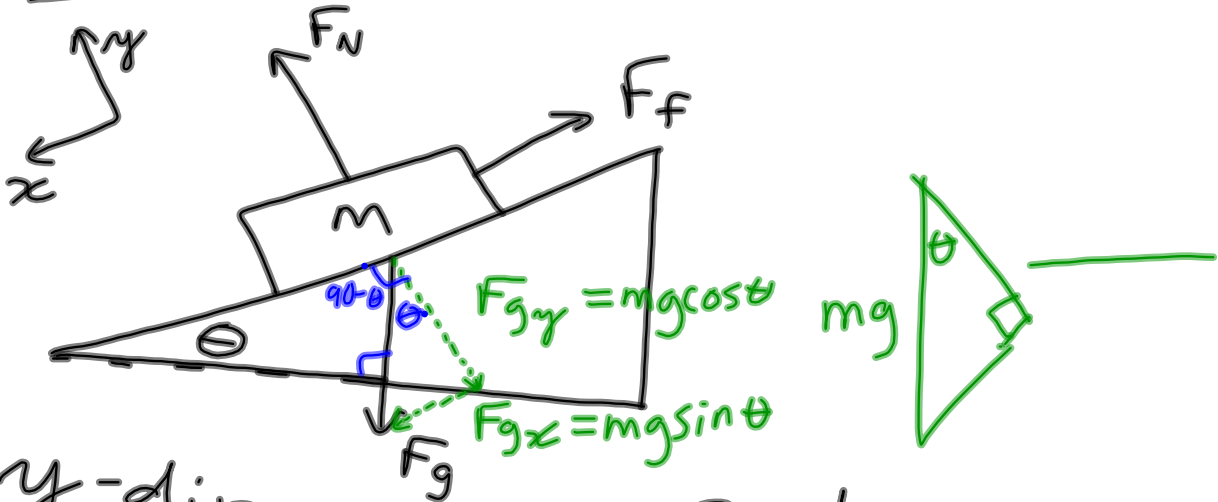
$$F_{NET} = ma = (0.1)(3.22) = 0.322 \text{ N}$$

$$F_{NET} = F_{T2} - F_{T1} - F_f$$

$$0.322 = 2.142 - F_{T1} - (0.4)(0.98)$$

$$F_{T1} = 2.142 - 0.322 - 0.392 = 1.428 \text{ N}$$

Ramps



y-dir

$$F_{NET} = F_N - F_{gy}$$

$$= F_N - mg \cos \theta$$

$$F_{NET} = 0$$

$$\therefore F_N = mg \cos \theta$$

x-dir

$$F_{NET} = F_{gx} - F_f$$

$$= mg \sin \theta - \mu F_N$$

$$= mg \sin \theta - \mu mg \cos \theta$$

$$F_{NET} = ma$$

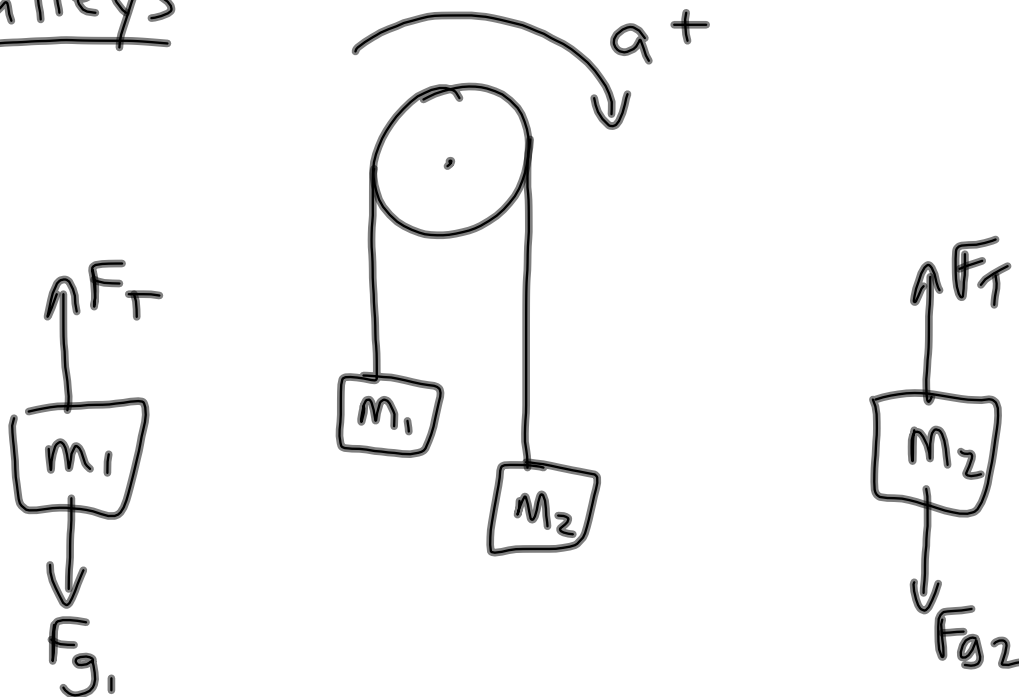
$$\therefore ma = mg \sin \theta - \mu mg \cos \theta$$

$$a = g \sin \theta - \mu g \cos \theta$$

\uparrow
 \vec{a} due to gravity
 as $\theta \uparrow$, this \uparrow

\uparrow
 retarding due to friction
 as $\theta \uparrow$, this \downarrow

Pulleys



$$F_{NET} = F_T - F_{g_1}$$

$$F_{NET} = m_1 a$$

$$m_1 a = F_T - m_1 g$$

$$F_T = m_1 a + m_1 g$$

$$= m_1 (a + g)$$

$$F_{NET} = F_{g_2} - F_T$$

$$F_{NET} = m_2 a$$

$$m_2 a = m_2 g - F_T$$

$$m_2 a = m_2 g - m_1 (a + g)$$

Ramps w/ pulleys

Determine \vec{a} & F_T

y-dir

$$F_{NET} = 0$$

$$F_{NET} = F_N - mg \cos 30$$

$$\therefore F_N = mg \cos 30$$

$$= (10)(9.8) \cos 30$$

$$= 84.9 \text{ N}$$

x-dir

$$F_{NET} = F_T - mg \sin 30 - F_f$$

$$= F_T - (10)(9.8) \sin 30 - \mu F_N$$

$$= F_T - 49 - (0.2)(84.9)$$

$$= F_T - 66$$

$$F_{NET} = ma$$

$$\therefore 10a = F_T - 66$$

Free-body diagram for 12 kg block:

$$F_{NET} = 12a$$

$$F_{NET} = F_g - F_T$$

$$12a = 117.6 - F_T$$

Substitution:

$$10a = 117.6 - 12a - 66$$

$$a = 2.35 \frac{\text{m}}{\text{s}^2}$$

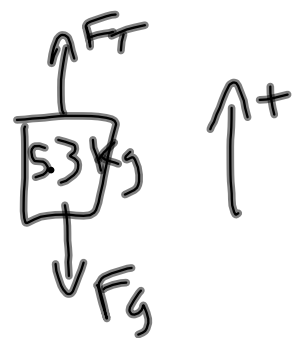
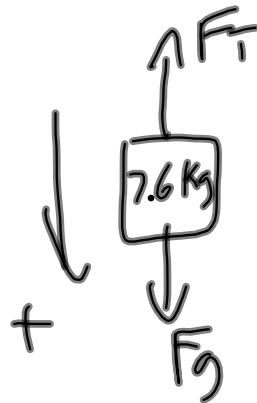
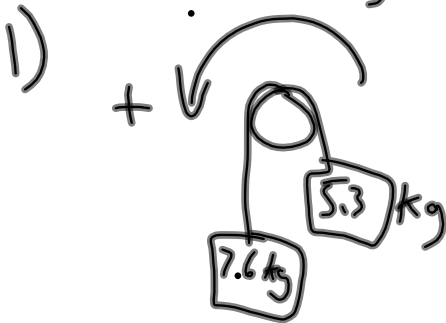
$$23.5 = F_T - 66$$

$$89.5 = F_T$$

- FBDs

- $\Sigma F = F_{NET}$
 - $ma = F_{NET}$ } each component

- tie in objects somehow (common \vec{a} , F_T ...)



$$F_{NET} = F_g - F_T$$

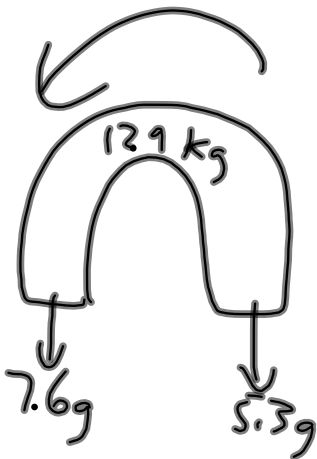
$$ma = (7.6)(9.8) - F_T$$

$$7.6a = 74.5 - F_T$$

$$F_{NET} = F_T - F_g$$

$$5.3a = F_T - 51.9$$

$$F_T = 5.3a + 51.9$$



$$7.6a = 74.5 - (5.3a + 51.9)$$

$$12.9a = 74.5 - 51.9$$

$$a = \frac{22.6}{12.9} = 1.75 \frac{m}{s^2}$$

$$t = 1.2 \text{ s}$$

$$v_i = 0$$

$$7.6a = 74.5 - 5.3a - 51.9$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$d = \frac{1}{2} (1.75) (1.2)^2$$

$$= 1.26 \text{ m}$$

$$\vec{d} = 1.26 \text{ m } [\downarrow]$$

Diagram showing a 5.2kg block on a horizontal surface connected by a string over a pulley to an 8kg hanging block. The string makes a 34-degree angle with the horizontal. Free-body diagrams are shown for both blocks.

Free-body diagram for the 5.2kg block:

- Vertical forces: F_N (up), F_g (down), $F_T \sin 34^\circ$ (up).
- Horizontal forces: F_f (left), $F_T \cos 34^\circ$ (right).

Free-body diagram for the 8kg block:

- Vertical forces: F_T (up), F_g (down).

Equations for the 5.2kg block:

vert

$$F_{NET} = F_N + F_T \sin 34 - 5.2g$$

$$\therefore 0 = F_N + F_T \sin 34 - 5.2g$$

$$F_N = 5.2g - F_T \sin 34$$

Hor.

$$F_{NET} = F_T \cos 34 - F_f$$

$$5.2a = F_T \cos 34 - (0.27)(5.2g - F_T \sin 34)$$

$$= F_T \cos 34 - 1.4g + 0.27F_T \sin 34$$

$$5.2a = 0.829F_T - 13.72 + 0.151F_T$$

$$5.2a = 0.98F_T - 13.72$$

Equations for the 8kg block:

$$F_{NET} = F_g - F_T$$

$$8a = 78.4 - F_T$$

$$F_T = 78.4 - 8a$$

Substitution and solution:

$$5.2a = 0.98(78.4 - 8a) - 13.72$$

$$5.2a = 76.8 - 7.84a - 13.72$$

$$13.04a = 63.1$$

$$a = 4.84 \frac{m}{s^2}$$

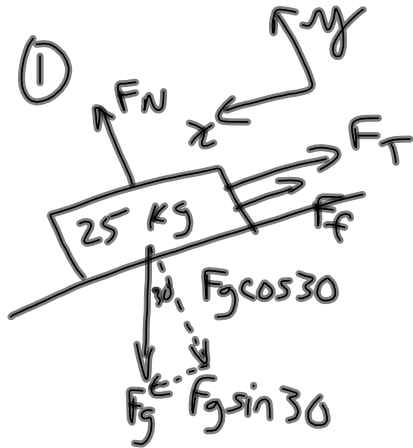
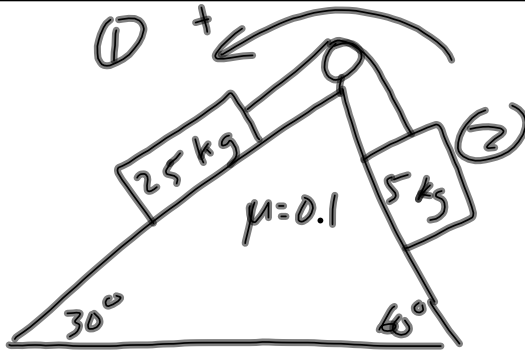
$$d = 0.67 m$$

Kinematic equation:

$$v_i = 0 \quad d = v_i t + \frac{1}{2} a t^2$$

$$0.67 = 2.42 t^2$$

$$t = 0.53 s$$



y-dir.

$$F_{NET} = 0$$

$$F_{NET} = F_N - mg \cos 30$$

$$\therefore F_N = (25)(9.8)(0.866)$$

$$F_N = 212 \text{ N}$$

x-dir

$$F_{NET} = 25a$$

$$F_{NET} = F_g \sin 30 - F_T - F_f$$

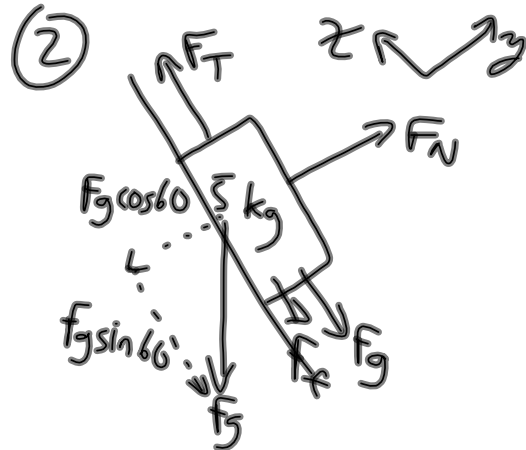
$$25a = 122.5 - F_T - (0.1)(212)$$

$$25a = 122.5 - F_T - 21.2$$

$$25a = 101.3 - F_T$$

$$25(1.88) = 101.3 - F_T$$

$$F_T = 53.3 \text{ N}$$



y-dir

$$0 = F_N - F_g \cos 60$$

$$F_N = 24.5 \text{ N}$$

x-dir.

$$5a = F_T - F_g \sin 60 - F_f$$

$$5a = F_T - 42.4 - (0.1)(24.5)$$

$$5a = F_T - 44.85$$

$$25a = 101.3 - F_T$$

$$5a = -44.85 + F_T$$

$$30a = 56.45$$

$$a = 1.88 \frac{\text{m}}{\text{s}^2}$$